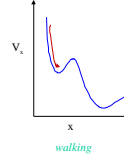


Molecular Dynamics Simulations

Searching Configuration Space

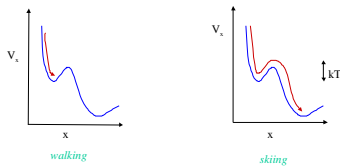
Energy minimization (EM)



They are always interested in the minimum !!!

Searching Configuration Space

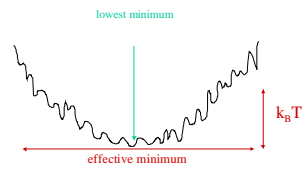
Energy minimization (EM) Molecular dynamics (MD)



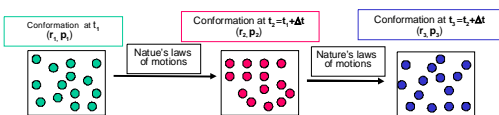
They are always interested in the minimum !!!

Molecular Dynamics: As a technique to search configuration space

The kinetic energy present in the systems allows it to surmount the energy barrier that are in the order of $k_B T$ per degree of freedom



The Molecular Dynamics method generates configurations applying Nature's Law of motions for atoms of a molecular system.



Solve Newton's equations of motion =
Time evolution of the system

Nature's law of motion

Newton's Equations of Motion

Force = Mass x Acceleration
or
Acceleration = Force/Mass

$$\frac{d^2 r_i}{dt^2} = \frac{F_i}{m_i}$$

Second-order differential equation

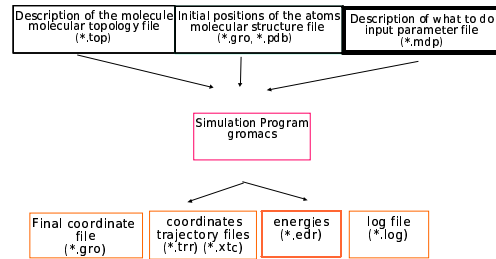
Force = -slope of the Potential → Force field

$$F_i = -\frac{\partial}{\partial r_i} V(r_1, r_2, \dots, r_N)$$

What governs the outcome of a MD simulation?

- starting configuration
- choice of degrees of freedom
- force field parameters
- boundary conditions**
- treatment of non-bonded interactions**
- integration time step**
- treatment of temperature and pressure**

Running a MD simulation



Keywords for non-bonded interactions and periodic boundary conditions in *.mdp file

```

;Interactions
coulombtype = cut-off ;treatment of electrostatic interactions
rcoulomb = 1.0 ;long range electrostatic cutoff
vdwtype = cut-off ;treatment of van der Waals interactions
rvdw = 1.0 ;long range van der Waals cutoff
;the neighbor list
nstlist = 10 ;Frequency to update the list.
ns_type = grid ;Method to determine list (simple, grid).
rlist = 1.0 ;cutoff for making list (short range forces).

;Periodic Boundary Conditions
pbc = xyz ;Periodic Boundary Conditions
    
```

Algorithms for Molecular Dynamics

Equation $\frac{d^2 r_i}{dt^2} = \frac{F_i}{m_i}$ (What do we have to solve) → Second-order differential equation

Newton's Equations of Motion

Solution: simple algorithms to integrate it in small time steps

For example: the leap-frog integrator

no derivative of force

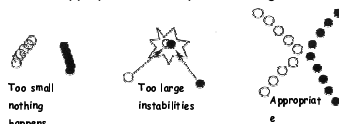
$$r_i(t+\Delta t) = r_i(t) + v_i(t+1/2\Delta t) \Delta t + O(\Delta t^3)$$

$$v_i(t+1/2\Delta t) = v_i(t-1/2\Delta t) + m^{-1} F(r_i(t)) \Delta t + O(\Delta t^3)$$

time ← time step

Choosing integration time step

- What is an appropriate time step for the integration?



System	Types of motion	Suggested time step
Rigid molecules	translation, rotation	5 fs
Flexible molecules, rigid bonds	translation, rotation, torsions	2 fs
Flexible molecules, flexible bonds	Translation, rotation, torsions, vibrations	1 or 0.5 fs

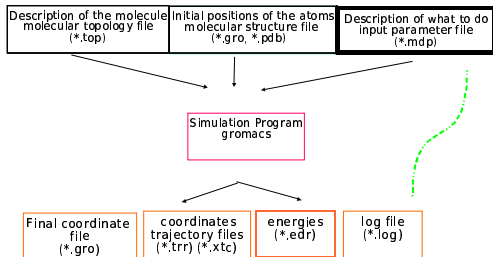
Keywords for MD algorithms in *.mdp file

```

title = MD simulation of .....
;Perform an MD simulation for 20 ps (example)
integrator = md ;Algorithm (md = molecular dynamics)
tinit = 0.0 ;starting time in picoseconds
dt = 0.002 ;time step in picoseconds
nsteps = 10000 ;number of steps (total simulation time)

;constraints
constraints = all-bonds ;Bond types to replace by constraints
    
```

Running a MD simulation



Keywords for output file control in *.mdp file

```

;Parameters to save data (what to write and when)
; frequency
nstxout = 100 ;coordinates to output trajectory file (*.trr)
nstvout = 100 ;velocities to output trajectory file(*.trr)
nstlog = 10 ;energies to log file(*.log)
nstenergy = 10 ;energies to energy file (*.edr)
nstxtcout = 10 ;coordinates to xtc trajectory (*.xtc)
;group(s) to write
xtc_grps = BUT SOL ;to xtc trajectory (*.xtc)
energygrps = BUT SOL ; to energy file (*.edr)
  
```

Temperature and Pressure

- Standard MD: number of particles N , volume V and total energy E_{tot} of the system are conserved (NVE ensemble)

$$E_{tot} = E_{potential} + E_{kinetic}$$

- Experiments are often performed at constant pressure P and temperature T (NPT ensemble)
- Approximations (cut-offs, integration) can lead to instabilities and thus energy and/or temperature variations

Temperature and pressure control needed

Temperature

- Temperature T related to the kinetic energy K of the system and therefore to the velocities

$$K = \sum_{i=1}^N \frac{1}{2} m_i v_i^2 = \sum_{i=1}^N \frac{p_i^2}{2m_i} = \frac{k_B T}{2} (3N - N_c)$$

- $3N - N_c$ is the number of degrees of freedom in the system
 - In particular N is the number of particles and N_c is the number of constraints on the system
- The temperature can thus be controlled by modifying the velocities of atoms and molecules in the system

Berendsen thermostat

- Temperature control by weak coupling to an external reference temperature bath
 - Velocities are scaled at a rate proportional to the temperature difference

$$\frac{dT}{dt} = \tau_T^{-1} (T_{bath} - T(t)) \quad \tau_T \text{ is a coupling parameter}$$

- Exponential decay toward reference temperature
- The scaling factor λ becomes:

$$\lambda = [1 + \Delta t \tau_T^{-1} (T_{bath}/T(t) - 1)]^{-1/2} \quad \Delta t \text{ integration time step}$$

Pressure

- The pressure is related to the volume of the system and the interaction between particles

Ideal gas: $PV = Nk_B T$

Real system: $PV = Nk_B T - \frac{1}{3k_B T} \sum_{i=1}^N \sum_{j=i+1}^N \vec{r}_{ij} \cdot \vec{f}_{ij}$

- The second term is the virial describing the contribution due to the forces between the particles
- Can easily be calculated in MD when calculating the forces

- Pressure can be controlled by varying the volume of the system and scaling the position of the molecules

Berendsen barostat

- Pressure can be controlled in a similar way as T by **weak coupling** to an external pressure bath with the rate of change given by:

$$dP/dt = \tau_p^{-1} (P_{ref} - P(t))$$

- Pressure can be adjusted by scaling the volume by a factor λ and the coordinate by $\lambda^{1/3}$

$$\lambda = 1 - \kappa \Delta t / \tau_p (P_{ref} - P(t))$$

where κ is the isothermal compressibility

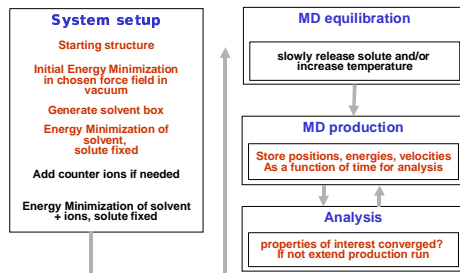
Keywords for temperature and pressure control in *.mdp file

```

;Temperature coupling at T=333 K (example )
tcoupl = berendsen ;Temperature coupling scheme
tc-grps = BUT SOL ;couple which group
tau_t = 0.1 0.1 ;relaxation time
ref_t = 333 333 ;reference temperature (K)

;Pressure coupling
Pcoupl = berendsen ;pressure coupling scheme
tau_p = 0.5 ;pressure relaxation time
compressibility = 4.5e-5 ;compressibility of system
ref_p = 1.0 ;reference pressure (atm)
    
```

Example of a simulation setup



MD simulations of butane in water solution at constant temperature and pressure

•Create the parameter file for around 500 ps simulation (using 2 fs time step) at the following simulation conditions:

- Constant temperature (T=300 K);
Constant pressure (p= 1 atm);
- Constant temperature (T=350 K);
Constant pressure (p= 1 atm).

•Run one MD simulation for each temperature.

Tips:
Use different directories for each simulation.
Use **top** to check that your simulations are running
Use **df** to check that disk space

Files we need for the MD simulation in water of butane at constant temperature and pressure.

- Geometry file** (*.gro or *.pdb): the output file of the minimizations performed in water solution: *confout.gro*.
- Corrected **topology file** for all-atom force field (butane.top)
PS: include "water.itp" and check the total number of water molecule at the end of the file
- Water topology file**, water.itp.
- Force field files** (ff.itp and ffb.itp)
- Parameter file** for molecular dynamics simulation in water
Fill the file md.mdp with the correct keywords

Check that the molecular dynamics simulation is equilibrated.

- Use the tools *g_energy* to extract the **temperature** and the **pressure** of the system from the energy file (ener.edr) using
g_energy -f ener.edr -o t.xvg and
g_energy -f ener.edr -o p.xvg
Plot t.xvg and p.xvg file (output of *g_energy*) using *xmgrace t.xvg* and *xmgrace p.xvg*.
- After how many ps do the **temperature** and the **pressure** reach a **plateau**? How large is the temperature at $t=0$ ps?
- Use the tools *g_energy* to extract **total energy** from the energy file *g_energy -f ener.edr -o energy.xvg*.
- Plot energy.xvg file (output of *g_energy*) using *xmgrace energy.xvg*. After how many ps does the **potential energy** reach a **plateau**?
- Is your simulation equilibrated before 500 ps? If not, run longer, if yes, after how many picoseconds?
- Visualise the trajectory using the software *vmd* (traj.xtc)